

# Modeling Variability and Uncertainty in Risk Assessment: a Case Study of *Salmonella* in Low $a_w$ Foods and its Use in Decision Making

Organized by: Microbial Modelling and Risk Analysis PDG

All opinions and statements are those of the individual making the presentation  
and not necessarily the opinion or view of IAFP



International Association for  
**Food Protection**®

# Speakers:

## FDA Center for Food Safety and Applied Nutrition

- Dr. Sofia Santillana Farakos  
    OAO/DRDA/Risk Analysis Branch
- Dr. Régis Pouillot  
    OAO/DRDA/Risk Analysis Branch
- Jenny Scott  
    Senior Advisor, the Office of Food Safety

## Moderator:

- Dr. Yuhuan Chen  
    FDA CFSAN/OAO/DRDA/Risk Analysis Branch  
    Chair of MMRA PDG (2014-2016)

# Facilitated Discussion

- **Questions should be submitted via the Text Chat section at the bottom of the screen.**
- **Q&A's to be held at the end of presentation**



# Modeling Variability and Uncertainty in Risk Assessment: a Case Study of *Salmonella* in Low $a_w$ Foods and its Use in Decision Making

Sofia Santillana Farakos

Régis Pouillot

Jenny Scott

IAFP WEBINAR June 8<sup>th</sup> 2016

## Before we start...

The information and conclusions presented in this webinar do not necessarily represent new Agency policy nor do they imply an imminent change in existing policy

## Outline of today's webinar

- Introduction
- *Salmonella* in low water activity foods
  - Prevalence and levels of contamination
  - Survival
  - Predictive modelling
- Modelling uncertainty and variability when assessing risk
  - The inference process
  - Simulation
  - Challenges
- Variability and uncertainty in risk management
  - Usefulness when making decisions

# Variability and Uncertainty

## Variability

### Heterogeneity

- Not reduced by additional data
- May be better characterized
- Growth, inactivation, serving size, ...

## Uncertainty

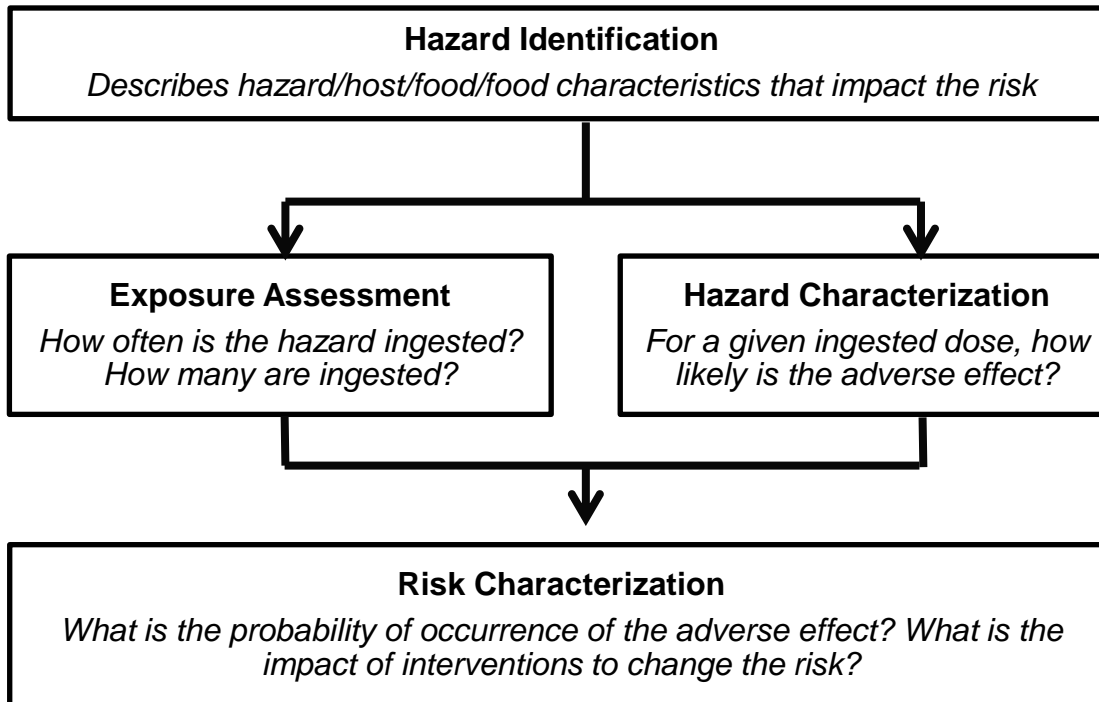
### The unknown

- Reduced by additional data
- Dose response, storage times, serving size, ...

**In many cases, factors are both variable and uncertain**

# Quantitative Microbial Risk Assessment

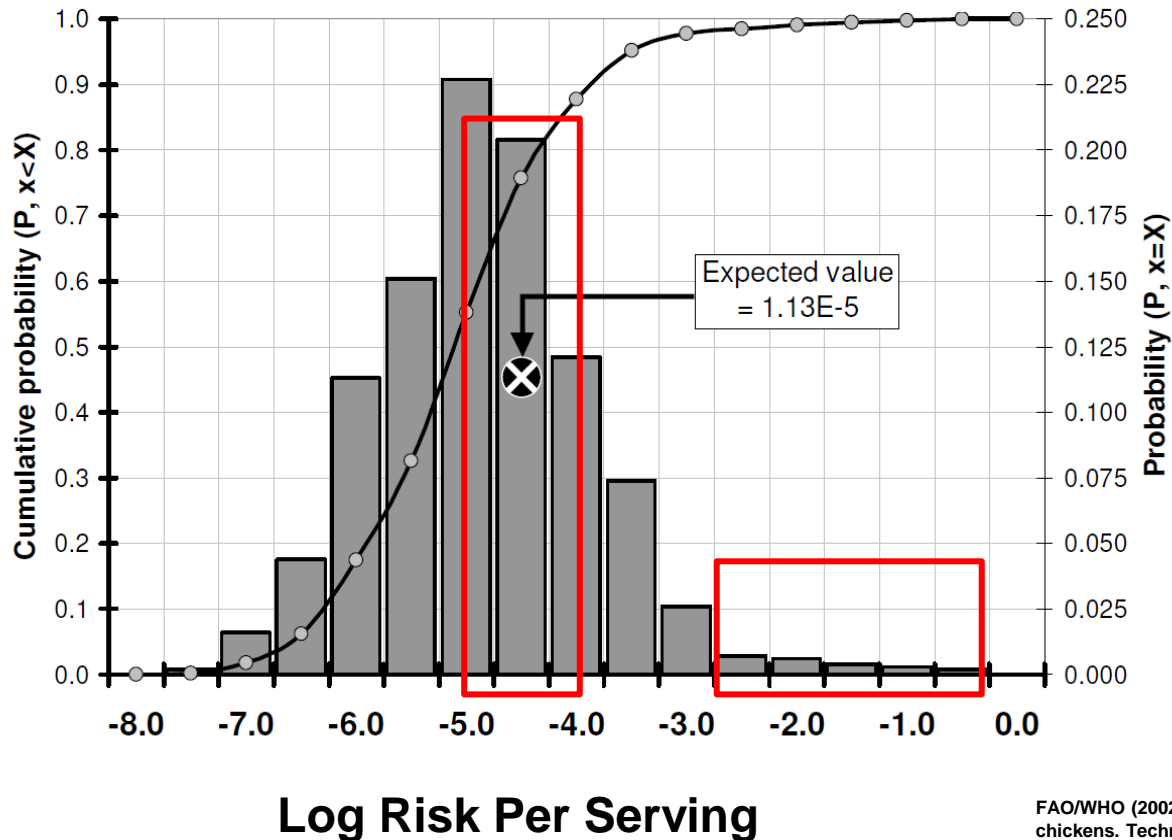
Assess the risk of illness from consumption of a product by a population



- Initial contamination
- Initial concentration
- Process characteristics
- Storage conditions
- Serving size
- Dose
- Dose Response
- Etc.



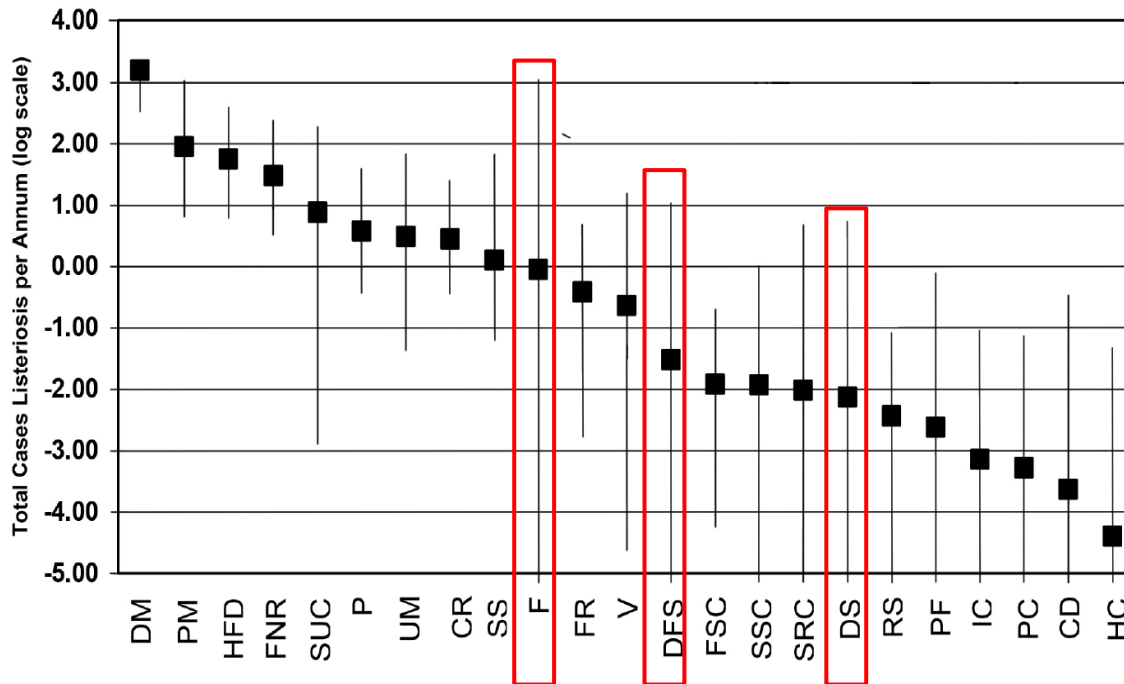
# Quantitative Microbial Risk Assessment: An example



**Understanding extremes**  
**CAN HELP RISK**  
**MANAGEMENT**

# Variability and Uncertainty in Risk Assessment

FDA/FSIS (2003).  
Quantitative assessment of the relative risk to public health from foodborne *Listeria monocytogenes* among selected categories of ready-to-eat foods.  
<http://www.fda.gov/Food/FoodScienceResearch/RiskSafetyAssessment/ucm183966.htm>

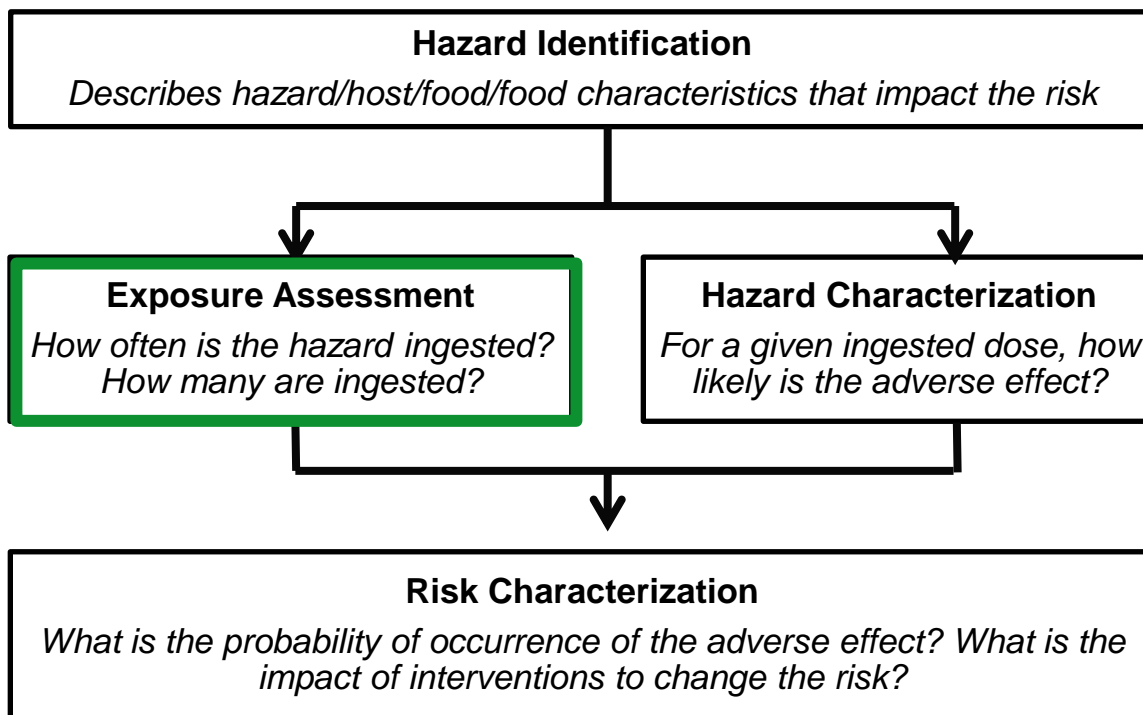


DM = Deli meats; PM = Pasteurized Fluid Milk; HFD = High Fat and Other Dairy Products;  
FNR = Frankfurters (not reheated); SUC = Soft Unripened Cheese; P= Pâté and Meat Spreads;  
CR = Cooked Ready-To-Eat Crustaceans; UM= Unpasteurized Fluid Milk; SS= Smoked Seafood;  
F = Fruits; FR = Frankfurters (reheated); V = Vegetables; DFS= Dry/Semi-dry Fermented Sausages;  
FSC = Fresh Soft Cheese; SSC = Semi-soft Cheese; SRC = Soft Ripened Cheese; DS = Deli-type Salads;  
RS = Raw Seafood; PF = Preserved Fish; IC= Ice Cream and Frozen Dairy Products; PC = Processed Cheese; CD = Cultured Milk Products; HC = Hard Cheese.



# *Salmonella* in low $a_w$ foods

# Salmonella in low $a_w$ foods: Contamination level



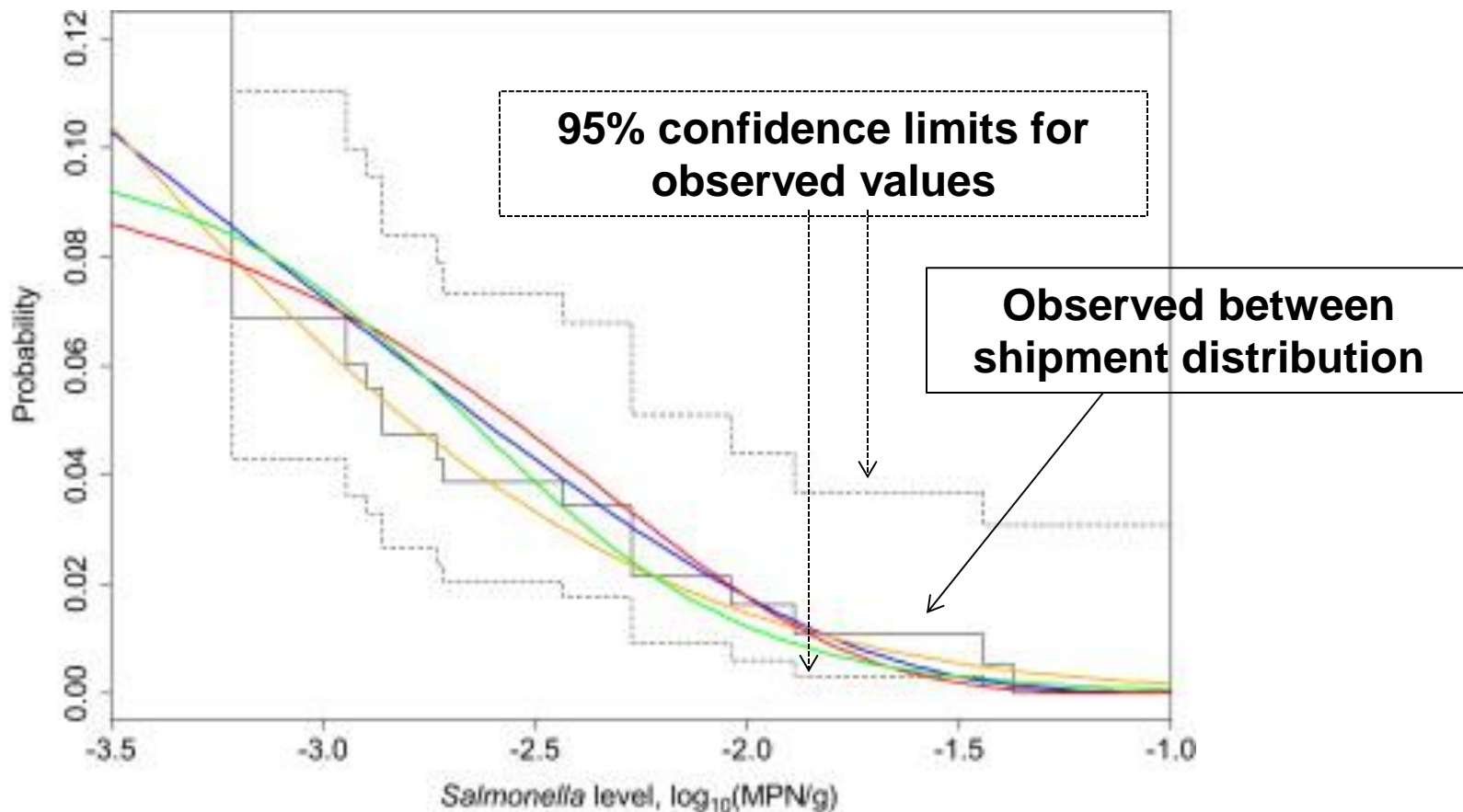
- Prevalence

## Contamination level

- Survival
- Growth
- Dose-Response
- Consumption

- Variability and uncertainty
- From year to year, from lot to lot, intra lot

# Salmonella in sesame seeds; Variability

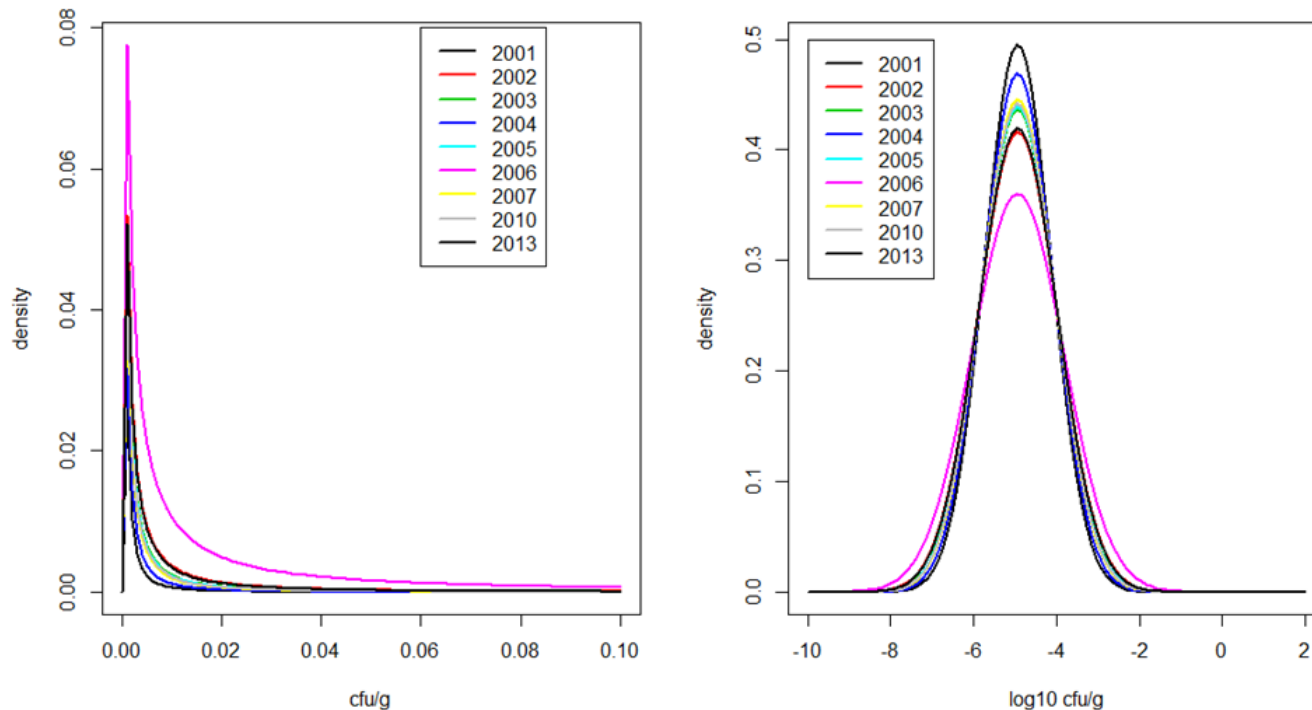


# Salmonella in almonds; Variability

**Intra Lot: Poisson distribution**

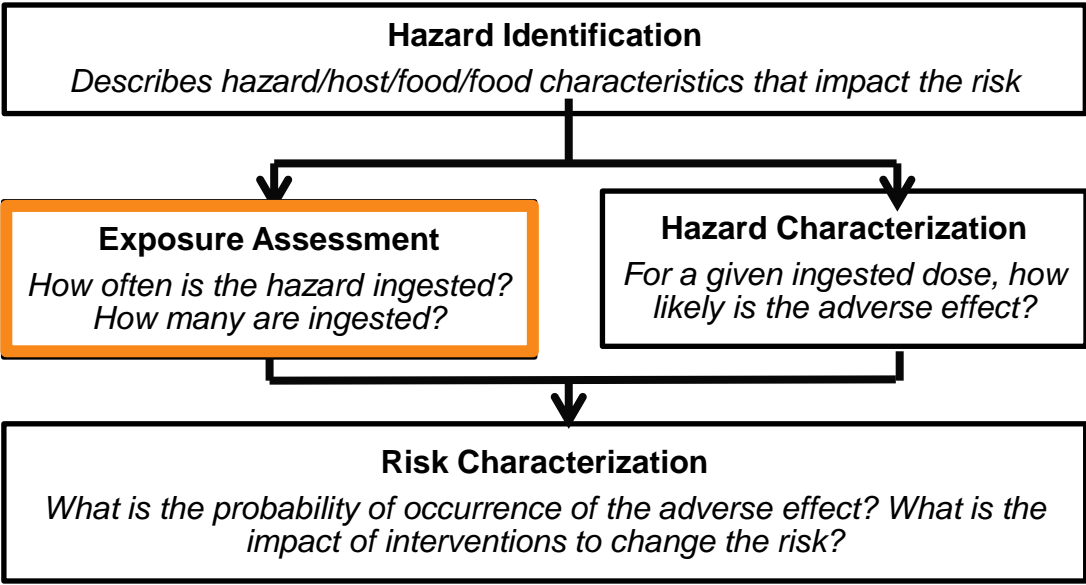
**Inter Lot: Log normal distribution**

**Year to year: same mean of the log, varying standard deviation**



Probability density functions of *Salmonella* contamination as predicted by the model.

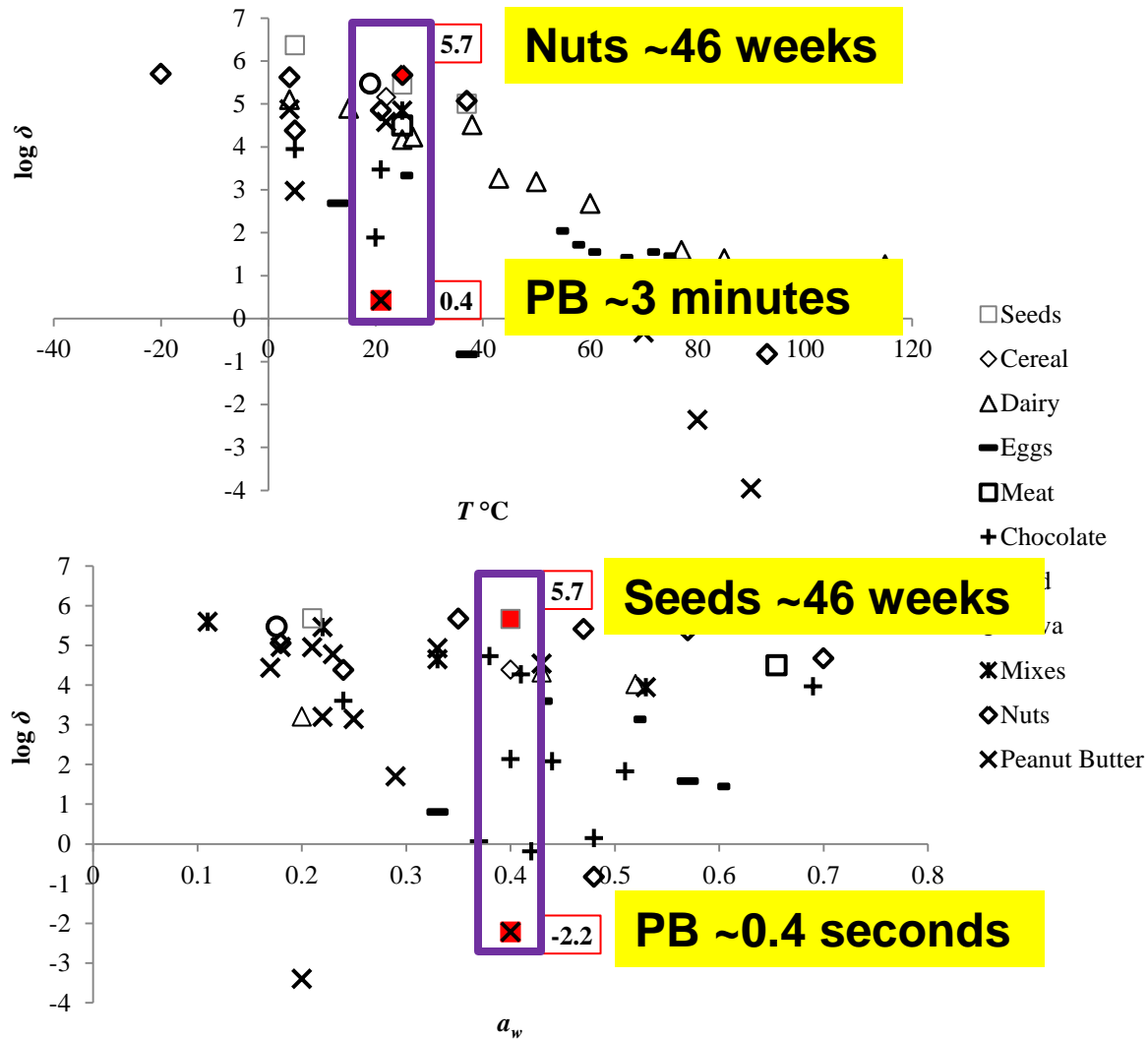
# Salmonella in low $a_w$ foods- Survival Data



- Prevalence
- Contamination level
- **Survival**
- Growth
- Dose-Response
- Consumption

Variability and Uncertainty in survival:

- Experimental conditions
- Strain
- Temperature
- $a_w$
- Food composition
- Survival model parameters

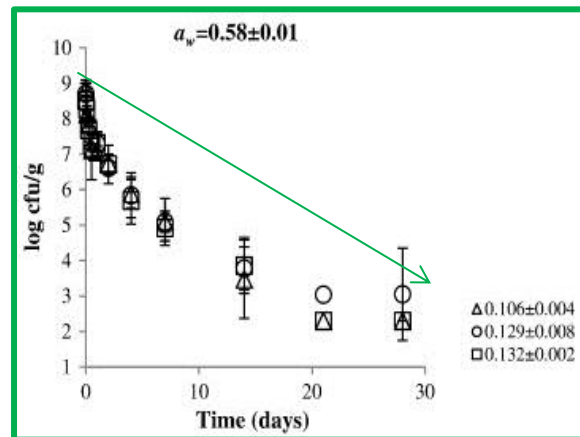
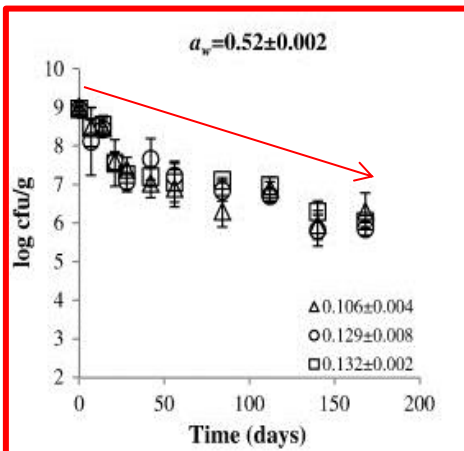
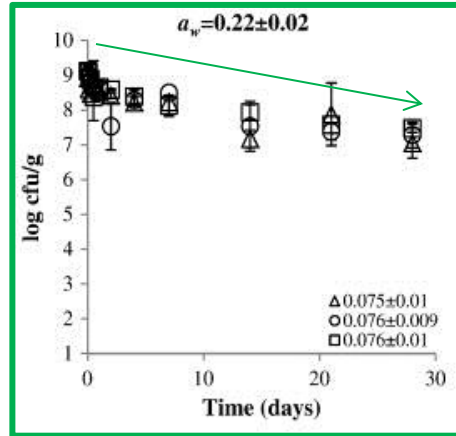
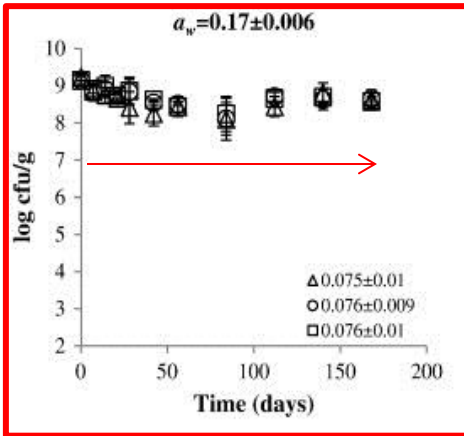




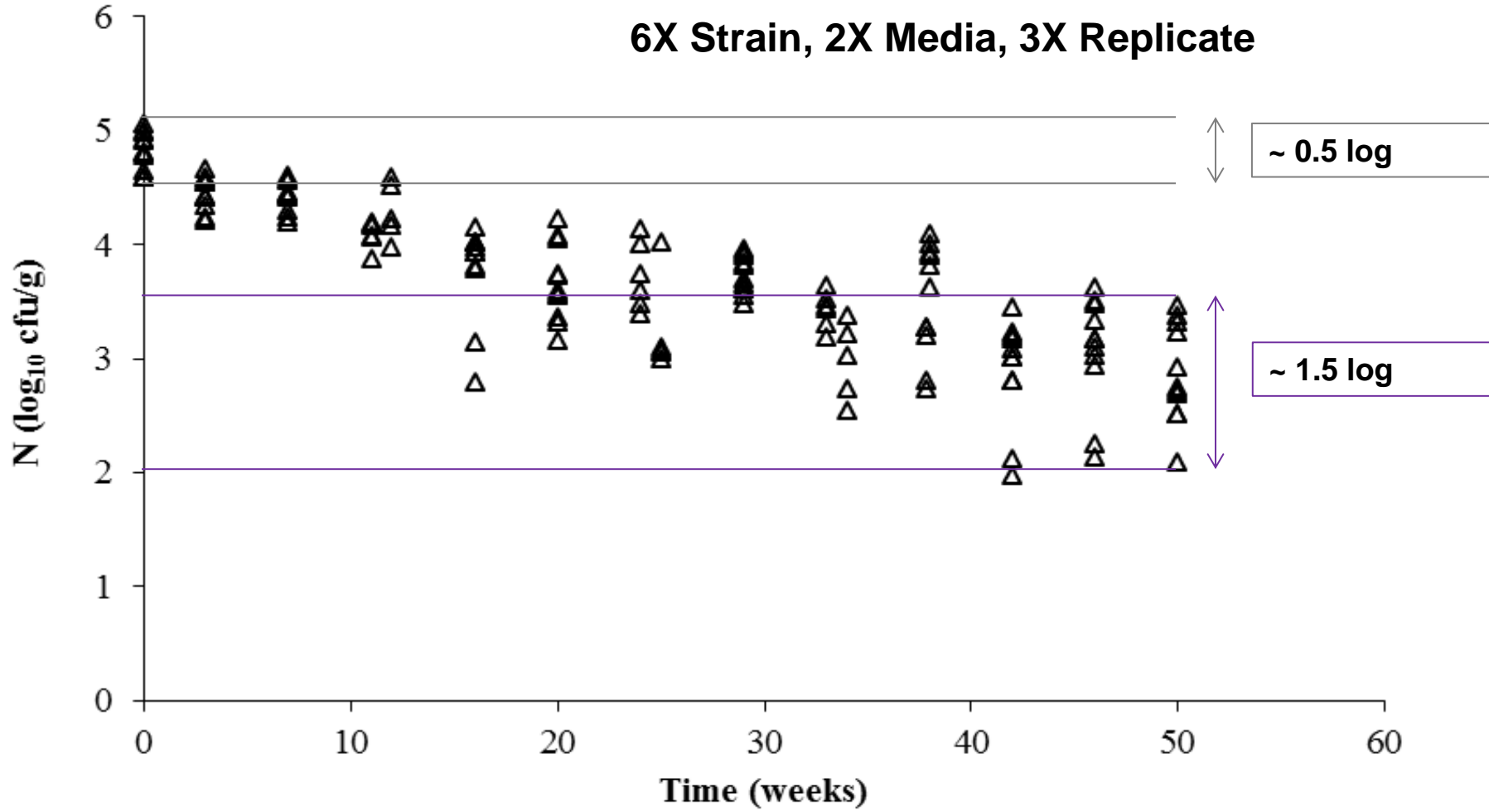
## Salmonella spp. survival at various T and $a_w$ on whey protein powder

21 °C

50 °C

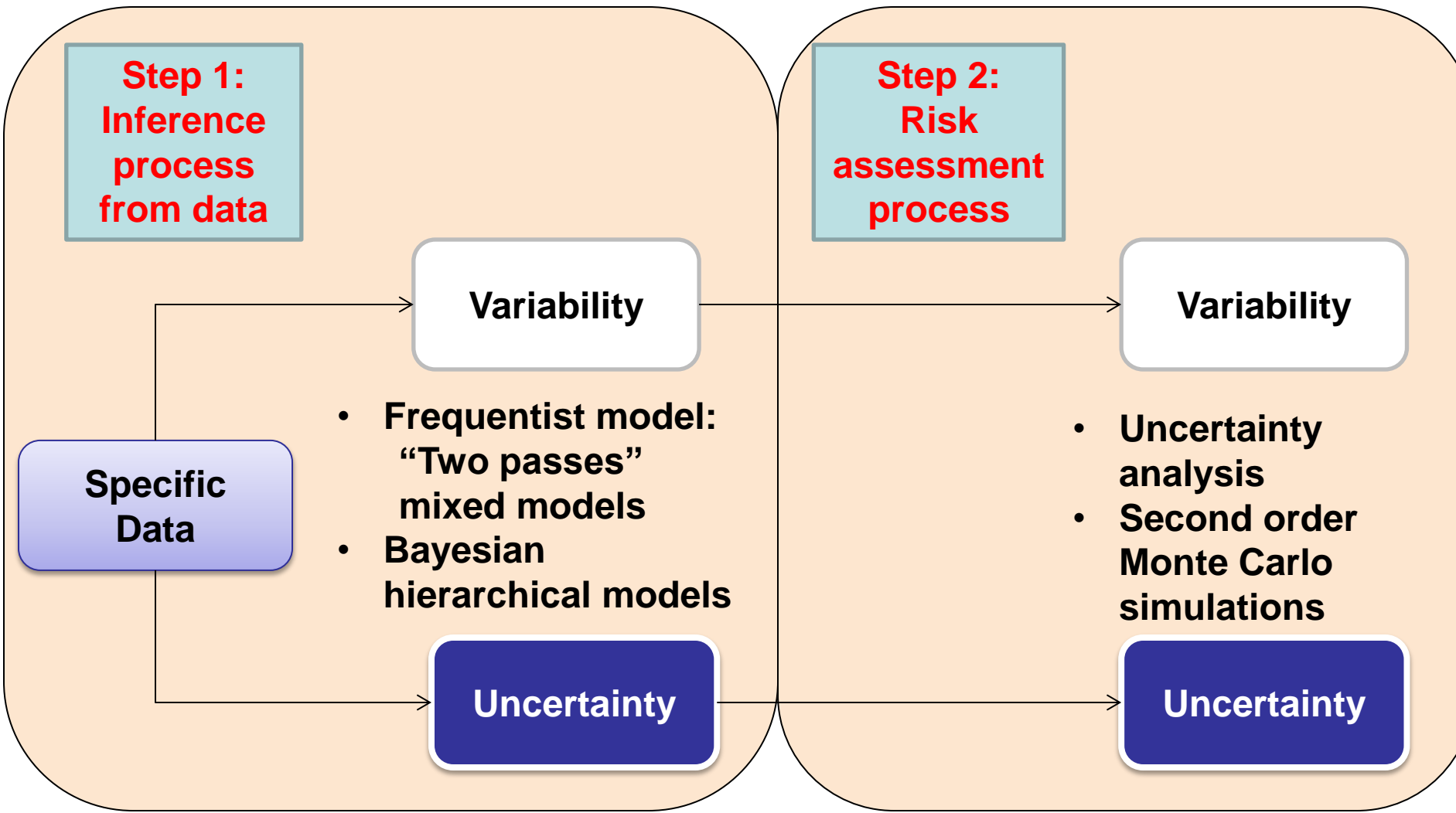


### 6X Strain, 2X Media, 3X Replicate





How do we model this variability and uncertainty for use in risk assessment?



**(One pass: Bayesian model)** (see Albert et al., 2008)

# Inference: Frequentist

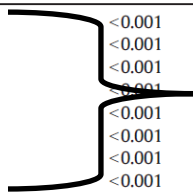
- Two passes (example: inactivation data)
  - Obtain data from representative situations (strain, stress, ...)
  - Model individual datasets for each strains/conditions → get a set of parameters
  - Parameter variability distribution derived from this set of model parameters

1170

E. Lambertini et al. / Food Research International 45 (2012) 1166–1174

**Table 2**  
Decline of *Salmonella* on almond kernels at different temperatures, modeled with linear and exponential functions.

Temperature (°C)	Serotype	Trial duration (days)	Inoculum (log CFU/g)	Linear model <sup>a</sup>	
				Slope (log CFU/month)	p-value <sup>c</sup>
23	PT 30	171	7.1	-0.32	<0.001
	PT 30	336	8.5	-0.21	<0.001
	PT 30	559	7.9	-0.24	<0.001
	PT 30	161	7.3	-0.16	<0.001
	PT 30	161	4.8	-0.21	<0.001
	PT 30	161	3.1	-0.25	<0.001
	PT 30	161	1.2 <sup>d</sup>	-0.20	<0.001
	Cocktail <sup>e</sup>	172	5.8	-0.29	<0.001
	4	PT 30	171	7.2	-0.052
PT 30		336	8.5	-0.039	<0.001
PT 30		559	7.9	-0.018	<0.001
Cocktail <sup>e</sup>		172	5.8	-0.019	0.67
-20	PT 30	559	7.9	0.0027	0.45
	Cocktail <sup>e</sup>	172	5.8	-0.043	<0.001



Slope ~Normal(-0.0078388, 0.00178)

<sup>a</sup> The linear model was expressed as:  $\log(\text{concentration}) = \log(\text{initial concentration}) + \text{rate} \cdot \text{days}$ .

<sup>b</sup> The fitted exponential curve was expressed as:  $\log(\text{concentration}) = \text{plateau} + \text{span} \cdot \exp(-k \cdot \text{days})$ .

<sup>c</sup> The 95% confidence intervals never included zero, except for the last trial at 4 °C, and the first trial at -20 °C.

<sup>d</sup> The results of this trial were excluded from the calculation of the average reduction rate at 23 °C for risk assessment purposes, due to several non-detects.

<sup>e</sup> The *Salmonella* cocktail included the following serotypes: Enteritidis PT 30, Enteritidis PT 9c, Tennessee, Oranienburg, Anatum, and Montevideo (unpublished).

## Inference: Frequentist

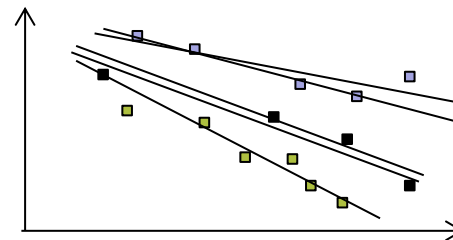
- One pass, directly from data
  - Mixed (linear or non linear) models are ways to consider population variability.
- Example: (log-)linear inactivation curves obtained from a set of strains  $i$

$$y_{ij} = \alpha_{ij} + \gamma_i X + \varepsilon_{ij},$$

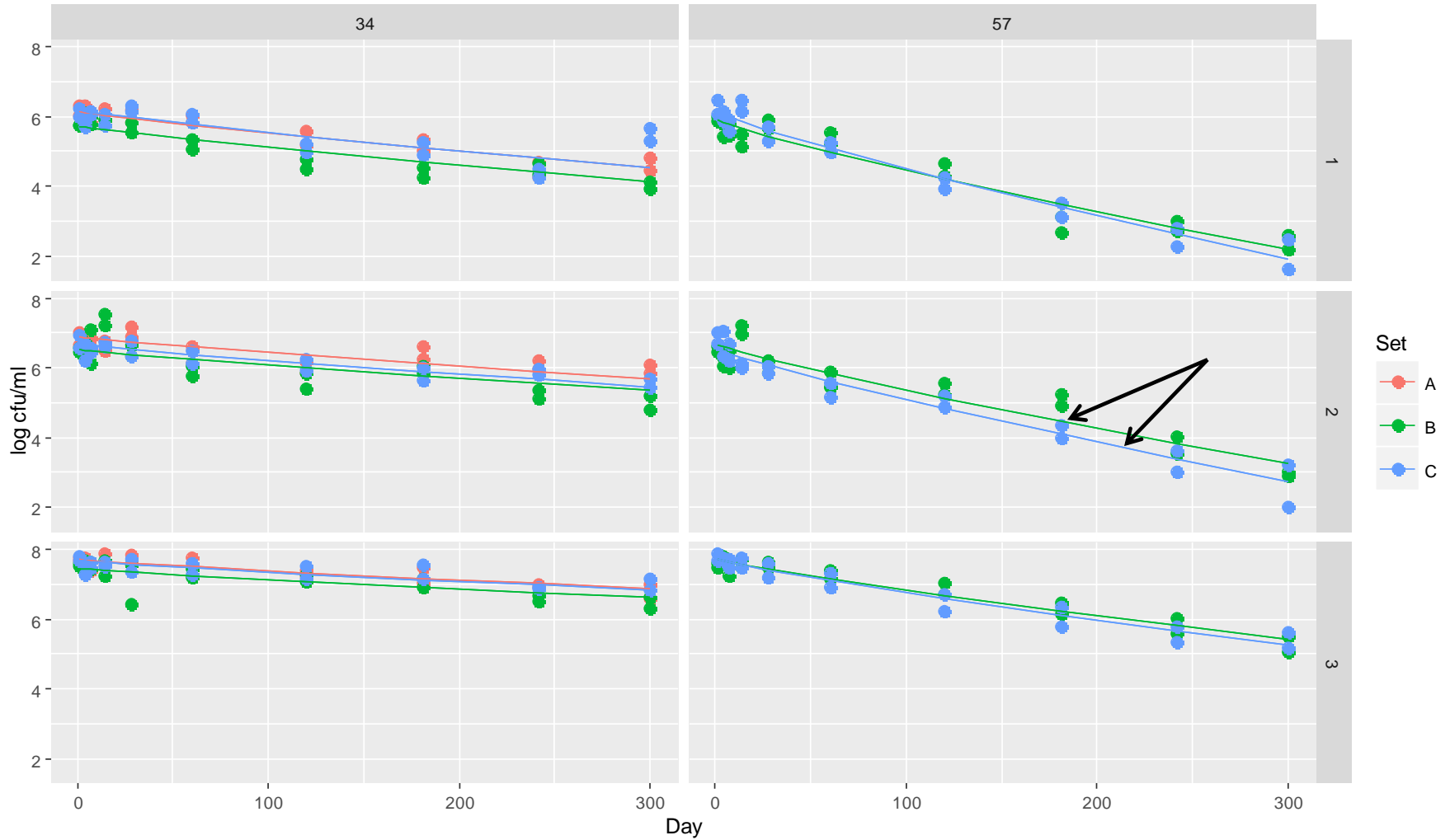
$$\gamma_i \sim \text{Normal}(\beta, \sigma_1^2)$$

$$\varepsilon \sim \text{Normal}(0, \sigma_2^2)$$

(rather than  $y_{ij} = \alpha_{ij} + \beta x + \varepsilon_{ij}$ ),



- The (log-)decrease varies from one strain to the other



Variability from replicate to replicate

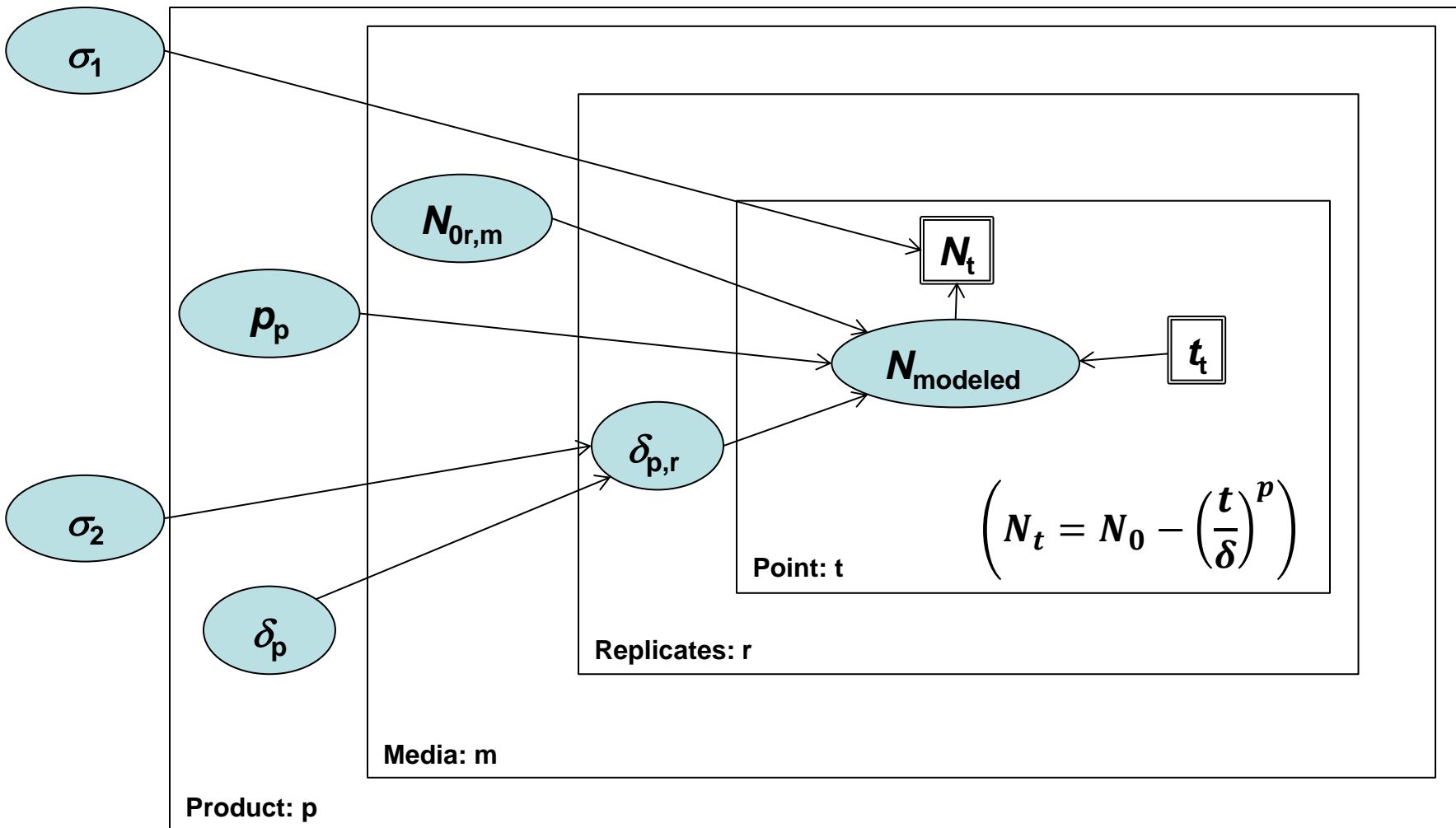
$$\delta_i \sim \text{Normal}(171, 4^2)$$

# Inference: Frequentist

- Uncertainty
  - Asymptotic distribution of estimators
    - Usually: normal
    - Difficulty to consider correlations
    - (sample size?)
  - Bootstrap
    - Pros: set of parameters that can be incorporated in the risk assessment model



# Inference: Bayesian



## Issue: Ad-hoc experimental design

- Variability
  - From population to population (strain-to-strain)
  - From day-to-day
  - From cell-to-cell within a population
- Need specific experimental design
  - No “cocktail” of strains, no “average” over replicates
  - Control of strain-to-strain, day-to-day conditions
  - See, e.g. den Besten et al., 2016
    - Experimental < Reproduction < Strain = Growth History = Population for *L. monocytogenes* inactivation

- Ad-Hoc data
  - Specific experimental design
  
- Literature data (meta analysis)
  - Representative strains?
  - How to consider lab-to-lab variability?

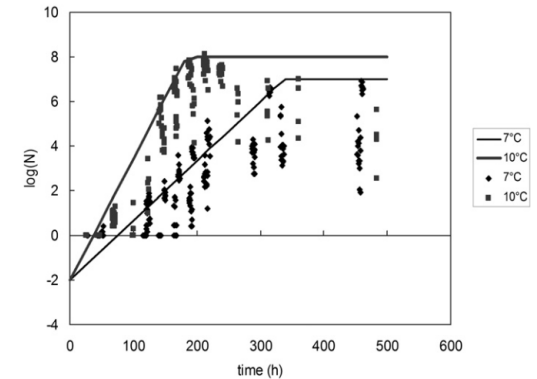


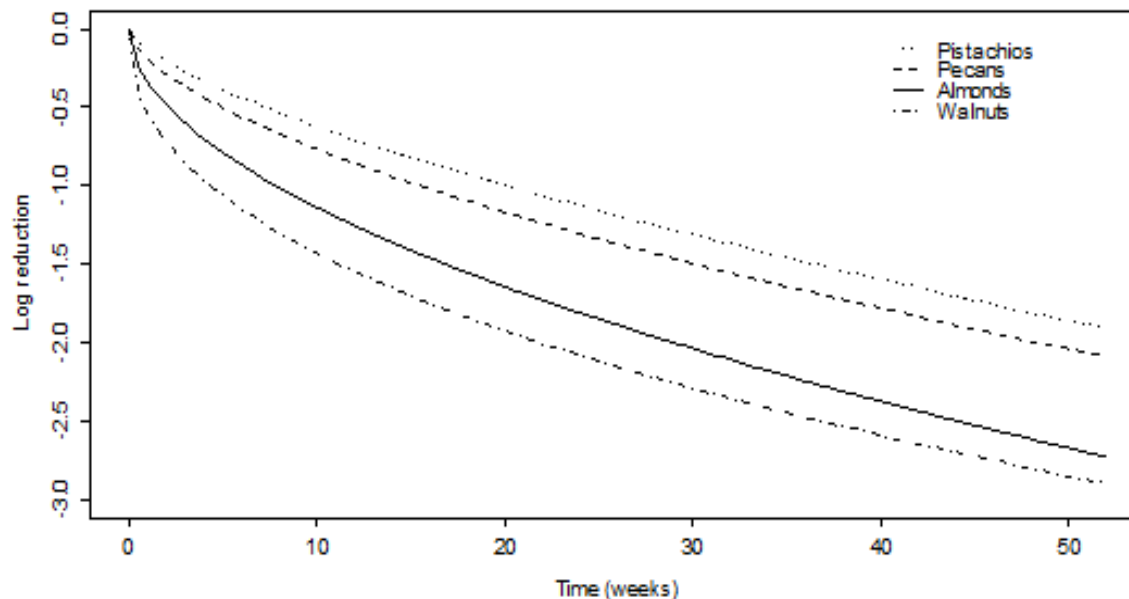
Fig. 3. Variability in the level of *Bacillus cereus* in several cartons of pasteurised milk stored at 7 and 10 °C (adapted from Zwietering et al., 1996).

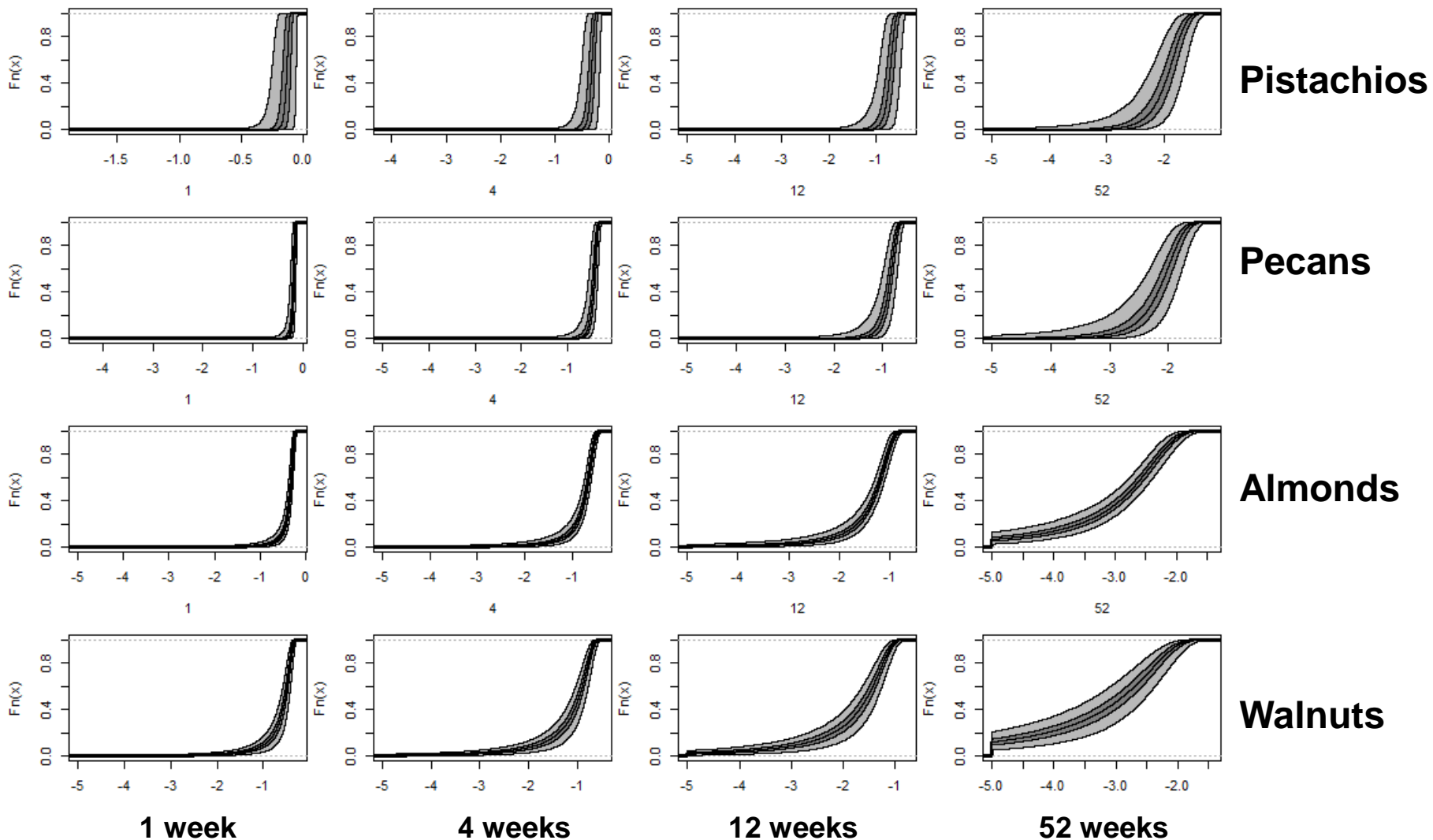
Study reference	Almond	Pecan	Pistachio	Walnut
Abd et al. (2012)	6	-	-	-
Beuchat and Mann (2010)	-	3	-	-
Blessington, Theofel and Harris (2013)	24	-	-	18
Blessington, Theofel, Mitcham, et al. (2013)	-	-	-	6
Brar et al. (2015)	-	4	-	-
Kimber et al. (2012)	6	-	6	-
Uesugi et al. (2006)	38	-	-	-

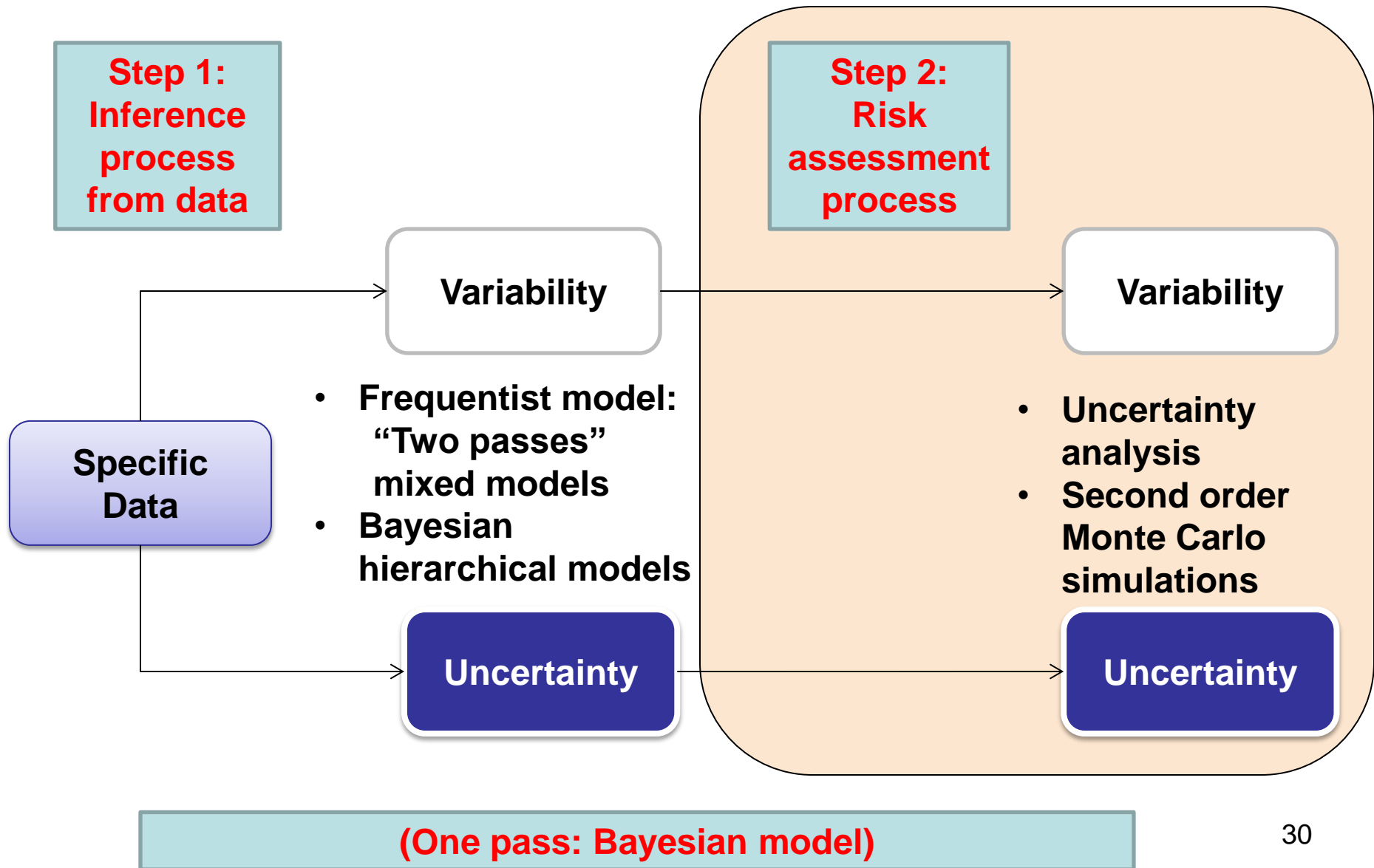
Example:  
*Salmonella*  
survival on  
tree nuts

$$\log_{10}(N_t) = \log_{10}(N_{0,e}) - (t/(\delta_s + r_\delta))^{p_s} + \varepsilon \quad (3)$$

where  $N_0$ ,  $N_t$ ,  $t$ ,  $\delta$ ,  $\rho$ ,  $e$ , and  $\varepsilon$  are defined as above with  $s$  in  $\delta_s$  and  $p_s$  representing the tree nut, almonds, pecans, pistachios or walnuts, and with the random effect on  $r_\delta$  following  $Normal(0, \sigma_\delta)$ .

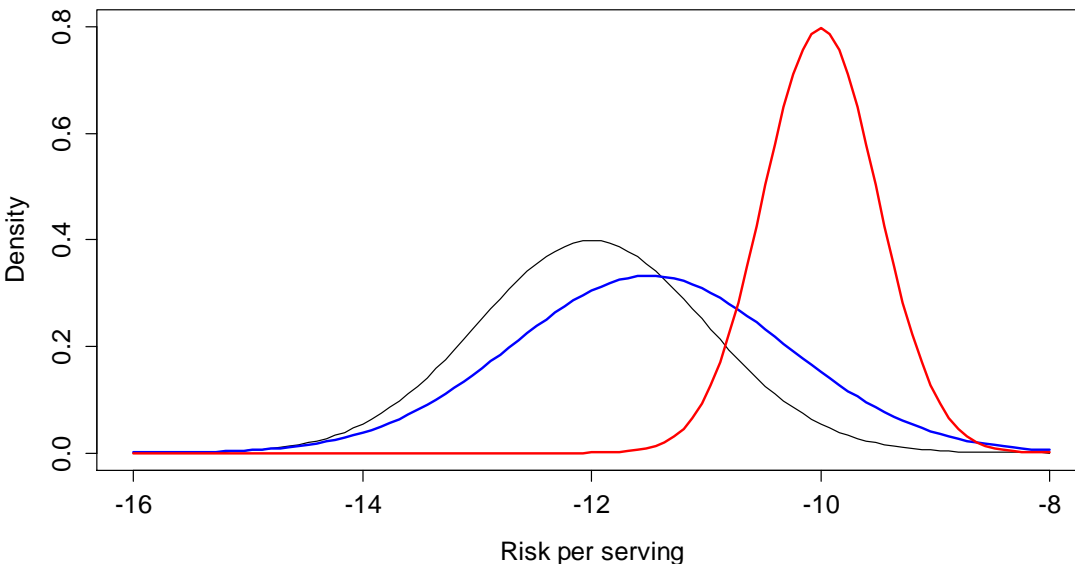






# Test alternative values for uncertain parameters / model

- Baseline
- Alternative #1: little impact
- **Alternative #2: high impact**



## Two-Dimensional (or Second Order) Monte-Carlo simulation

- Principle
  - Separation of the parameters according to the meaning of their dispersion
    - Variable parameters
      - Example: Portion Size (from individual to individual), Distribution of the contamination| mean contamination (from year to year)
    - Uncertain parameters
      - Example: Mean of the number of bacteria / 100g for a given year
  - Model Integration using Two Embedded Monte-Carlo Simulations
    - A Variability modeling embedded in an Uncertainty modeling

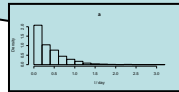
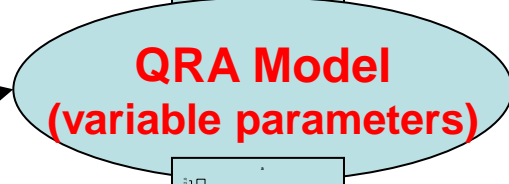
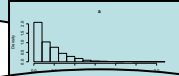
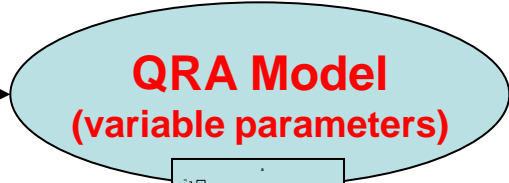


# Second-Order Monte Carlo Simulation

Uncertain parameter  $X$  (example: mean  $\log_{10}$  decrease / week)  
Fixed to a given random sample issued from the uncertainty distribution

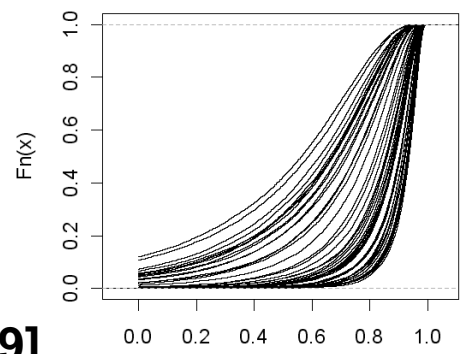
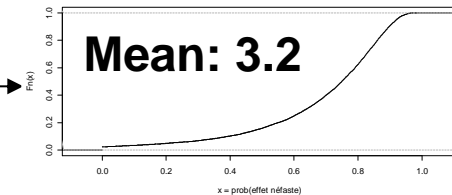
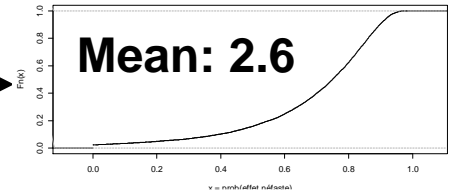
Uncertain parameter  $X$  (example: mean  $\log_{10}$  decrease / week)  
Fixed to a given random sample issued from the uncertainty distribution

...



...

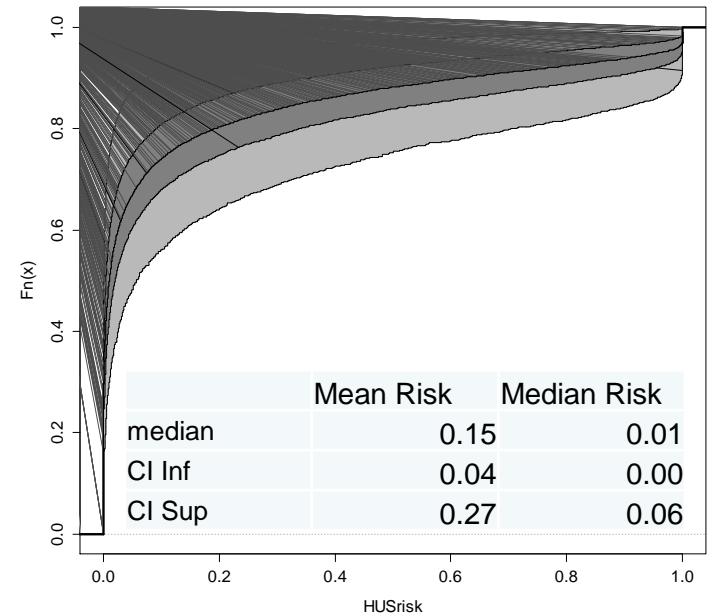
$N_u$  times...



$N_u$  Means: median 3.3, 2.5 and 97.5<sup>th</sup> percentiles [.2, 6.9]

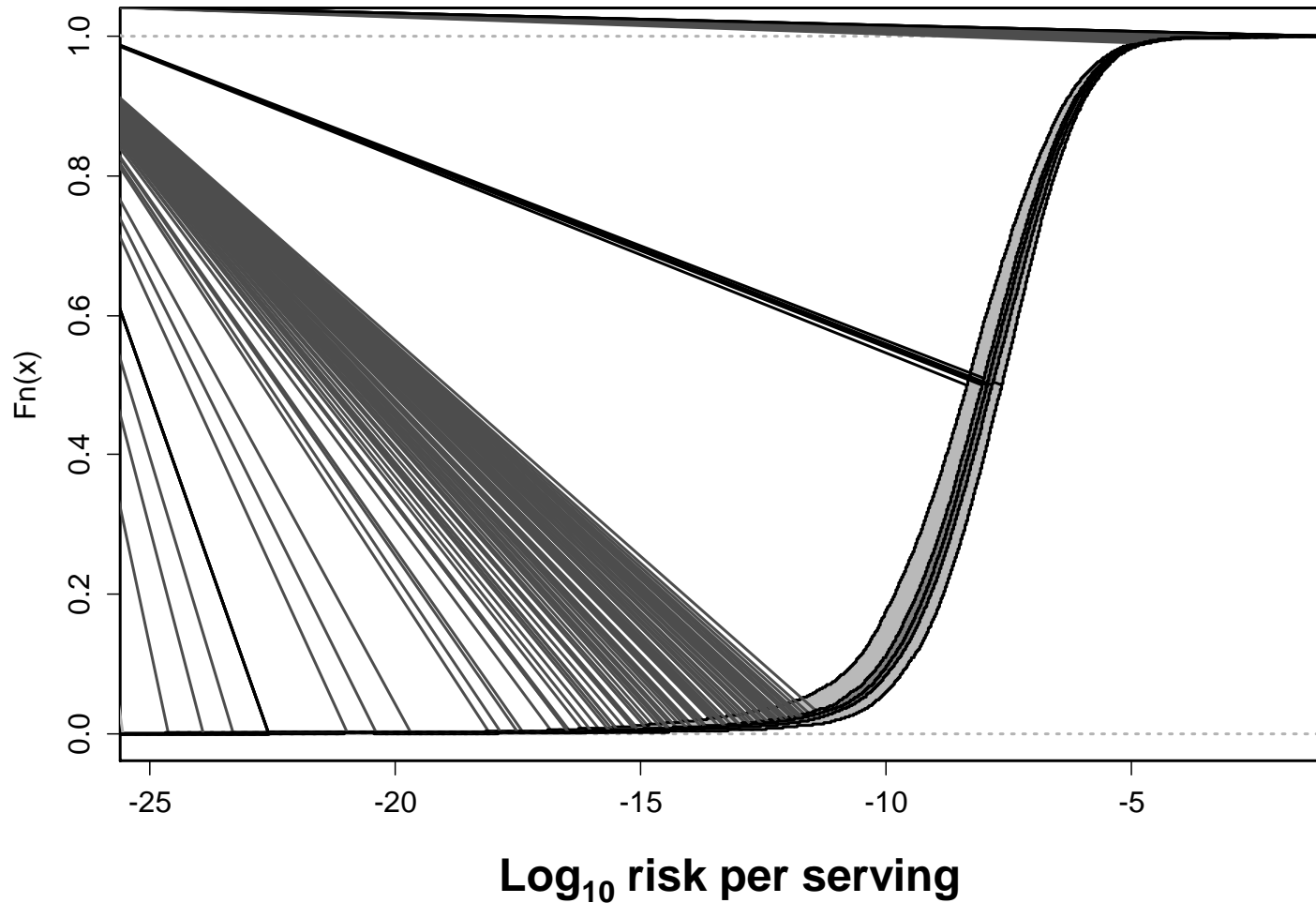
# In practice

- Separation of uncertainty and variability is not explicitly considered in most MC software used in QMRA
- Can be done in classical MC software using large matrices or use other tools
- 2D-MC simulation to be implemented in FDA-iRISK<sup>®</sup> 3.0
- R package *mc2d* “Ease the development of MC and 2D-MC in R”
  - (you specify if the distributions represent Uncertainty or Variability, then *mc2d* do the math for you)



**Variability cumulative distribution plots of the output of an *E. coli* model in ground beef model**

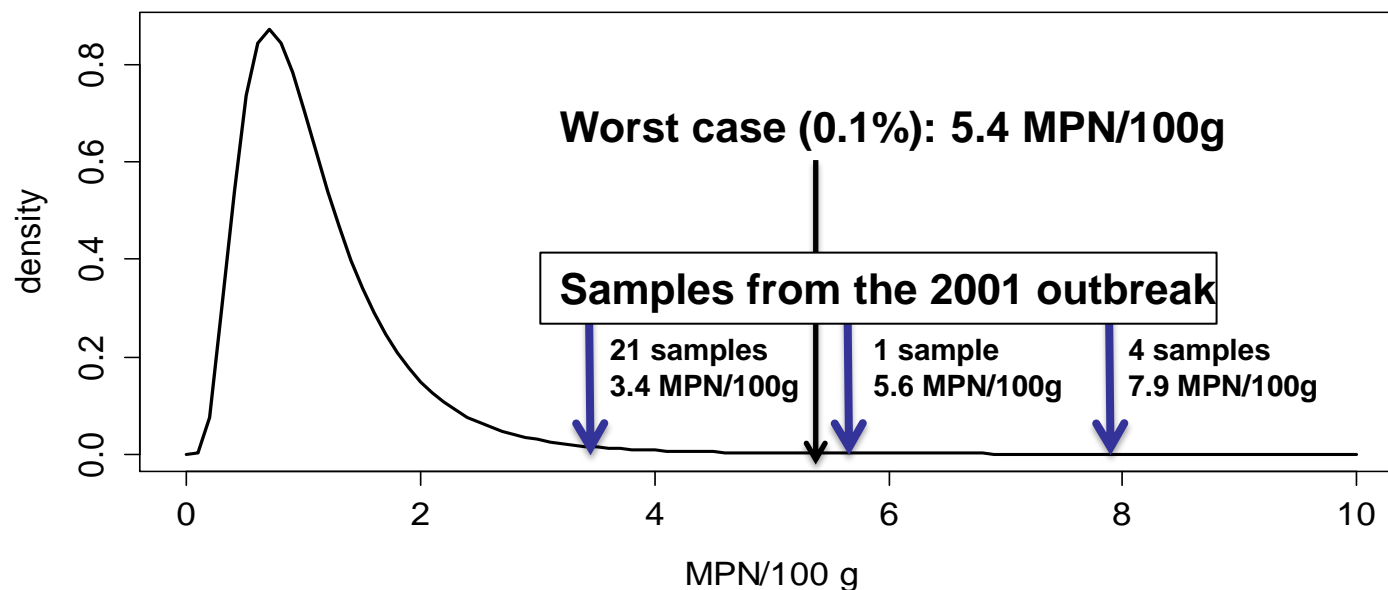
# Results



## Warning

- In this talk, we considered only data uncertainty within a given model
- Need to consider other sources of uncertainty
  - Scenario uncertainty
  - Model uncertainty
- May be much more important than the data uncertainty

# Salmonella in almonds



- The “outbreak situation” is not simply an extreme of the “usual situation”.
- Needed to consider separately “usual situation” and “outbreak situation”, as was done in this paper

# Conclusions

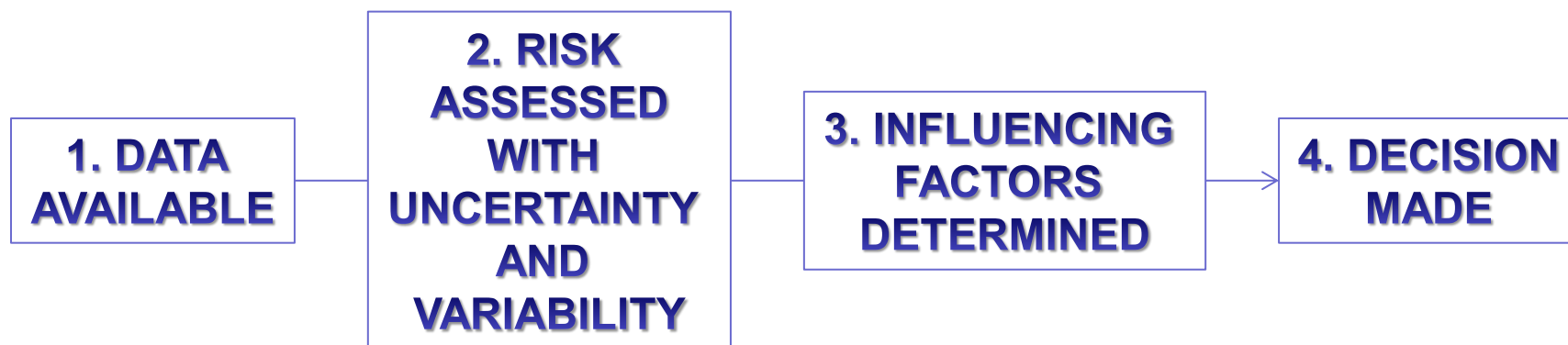
- Don't mix variability and uncertainty
  - Easiest way: consider variability only and test uncertainty for some major parameters
  - More complex methods available
  - Need carefully designed data collection for risk assessment purpose to consider proper variability
- Don't forget Scenario and Model uncertainty
  - Need to model “exceptional events” that are not the extreme of the usual distribution
    - May lead your whole risk
    - Frequency? Magnitude?



How can we use the modeled variability and uncertainty for decision making?

# Risk Management

**IDEALLY...**



**SITUATION RARELY IDEAL, ASSUMPTIONS HAVE TO BE MADE**



# How to make a decision?

Log reduction treatment ( $\log_{10}$ )	Estimated mean number of cases		
	Estimate	CI 95%	
0	100,000	10,000	1,000,000
1	10,000	1,000	100,000
2	1,000	100	10,000
3	100	10	1000
4	10	1	100
5	1	<1	10
6	<1	<1	<1

# Overall challenges in considering uncertainty and variability in risk analysis

- Risk assessors
  - Complicated process/ Not well understood
  - Feasibility
  - Lack of “easy-to-use” tools
- Risk managers
  - More difficult to handle
  - The uncertainty may be considered as “too large”
  - How to “draw a line”?
- Risk communication
  - More difficult to communicate
    - “So you are not certain?”

# References used

- Albert, I., E. Grenier, J. B. Denis and J. Rousseau (2008). "Quantitative risk assessment from farm to fork and beyond: a global Bayesian approach concerning food-borne diseases." Risk Anal **28**(2): 557-571.
- den Besten, H. M., D. C. Aryani, K. I. Metselaar and M. H. Zwietering (2016). "Microbial variability in growth and heat resistance of a pathogen and a spoiler: All variabilities are equal but some are more equal than others." Int J Food Microbiol.
- FAO/WHO (2002). Risk Assessment of *Salmonella* in eggs and broiler chickens. Technical report. Microbiological Risk Assessment Series, no 2. Rome, Food and Agriculture Organization of the United Nations and World Health Organization: 327
- Food and Drug Administration / Food Safety and Inspection Service (2003). Quantitative assessment of relative risk to public health from foodborne *Listeria monocytogenes* among selected categories of ready-to-eat foods, Food and Drug Administration, United States Department of Agriculture, Centers for Disease Control and Prevention: 541.  
<http://www.fda.gov/Food/FoodScienceResearch/RiskSafetyAssessment/ucm183966.htm>.
- Kimber, M. A., H. Kaur, L. Wang, M. D. Danyluk and L. J. Harris (2012). "Survival of *Salmonella*, *Escherichia coli* O157:H7, and *Listeria monocytogenes* on Inoculated Almonds and Pistachios Stored at 19, 4, and 24 C." J Food Prot **75**(8): 1394-1403.
- Lambertini, E., M. D. Danyluk, D. W. Schaffner, C. K. Winter and L. J. Harris (2012). "Risk of salmonellosis from consumption of almonds in the North American market." Food Research International **45**(2): 1166-1174.
- Pouillot, R., M.-L. Delignette-Muller, D. L. Kelly and J.-B. Denis (2015). The mc2d package. <https://cran.r-project.org/web/packages/mc2d/vignettes/docmcEnglish.pdf>.
- Santillana Farakos, S. M., R. Pouillot, N. Anderson, R. Johnson, I. Son and J. Van Doren (2016). "Modeling the survival kinetics of *Salmonella* in tree nuts for use in risk assessment." Int J Food Microbiol **227**: 41-50.
- Santillana Farakos, S. M., D. W. Schaffner and J. F. Frank (2014). "Predicting survival of *Salmonella* in low-water activity foods: an analysis of literature data." J Food Prot **77**(9): 1448-1461.
- Santillana Farakos, S.M., J.F., Frank, D.W., Schaffner (2013). "Modeling the influence of temperature, water activity and water mobility on the persistence of *Salmonella* in low-moisture foods." Int J Food Microbiol **166**: 280-293.
- Van Doren, J. M., R. J. Blodgett, R. Pouillot, A. Westerman, D. Kleinmeier, G. C. Ziobro, Y. Ma, T. S. Hammack, V. Gill, M. F. Muckenfuss and L. Fabbri (2013). "Prevalence, level and distribution of *Salmonella* in shipments of imported capsicum and sesame seed spice offered for entry to the United States: Observations and modeling results." Food Microbiology **36**(2): 149-160.
- Zwietering, M. H. (2015). "Risk assessment and risk management for safe foods: Assessment needs inclusion of variability and uncertainty, management needs discrete decisions." Int J Food Microbiol **213**: 118-123.

# Contact information for speakers

## FDA Center for Food Safety and Applied Nutrition

- [Sofia.SantillanaFarakos@fda.hhs.gov](mailto:Sofia.SantillanaFarakos@fda.hhs.gov)
- [Regis.Pouillot@fda.hhs.gov](mailto:Regis.Pouillot@fda.hhs.gov)
- [Jenny.Scott@fda.hhs.gov](mailto:Jenny.Scott@fda.hhs.gov)